

The combined $\nu_{\mu} \rightarrow \nu_e$ oscillations fit for the BDT analysis in MiniBooNE

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Introduction:

The Boosted Decision Tree (BDT) oscillations analysis in MiniBooNE uses the observed ν_{μ} -CCQE events to normalize and constrain its Monte Carlo prediction and systematic errors for the ν_e events via the construction of an error matrix which contains the correlations between the bins of the energy distributions of the two samples. This matrix is then used in a χ^2 minimization procedure to fit for the oscillation parameters. A description of the method is given and a few examples of fits are described.

The ν_{μ} -CCQE event sample:

Require the occurrence of 2 sub-events, the second of which is consistent with an electron from μ^- decay at rest. The reconstructed vertex of this electron must be within 100 cm from the reconstructed endpoint of the track of its parent μ^- . The μ^- event (1st sub-event) is required to occur inside the beam window and to fire more than 200 tank PMT's and less than 6 veto PMT's, while the e^- is required to fire less than 200 tank PMT's. The reconstructed vertex of the μ^- event must be within 500 cm from the tank center.

The BDT ν_e event sample:

Pre-selection requirements include the occurrence of a single sub-event inside the beam window, firing more than 200 tank PMT's and less than 6 veto PMT's, and a fiducial radius cut of 500 cm. A number of input variables containing information about the light patterns produced by the events in the oil are fed to a Boosted Decision Tree algorithm to produce a powerful PID output variable. PID cut values are optimized in each energy bin to maximize sensitivity to oscillations.

The χ^2 :

$$\chi^2 = \sum_i (N_i^{Data} - N_i^{MC}) M_{ij}^{-1} (N_j^{Data} - N_j^{MC})$$

$$N_i^{MC} = N_i^{MC}(\sin^2 2\theta, \Delta m^2), \quad i = E_{\nu}^{QE} \text{ bin}$$

The index i runs across the ν_{μ} and ν_e bins. Only the number of Monte Carlo ν_e events depend on the oscillation parameters. The matrix M contains all possible sources of error, systematic and statistical. Fit for a signal described by 2 ν oscillations::

$$P(\nu_{\mu} \rightarrow \nu_e) = \sin^2 2\theta \sin^2(1.27 \Delta m^2 L/E)$$

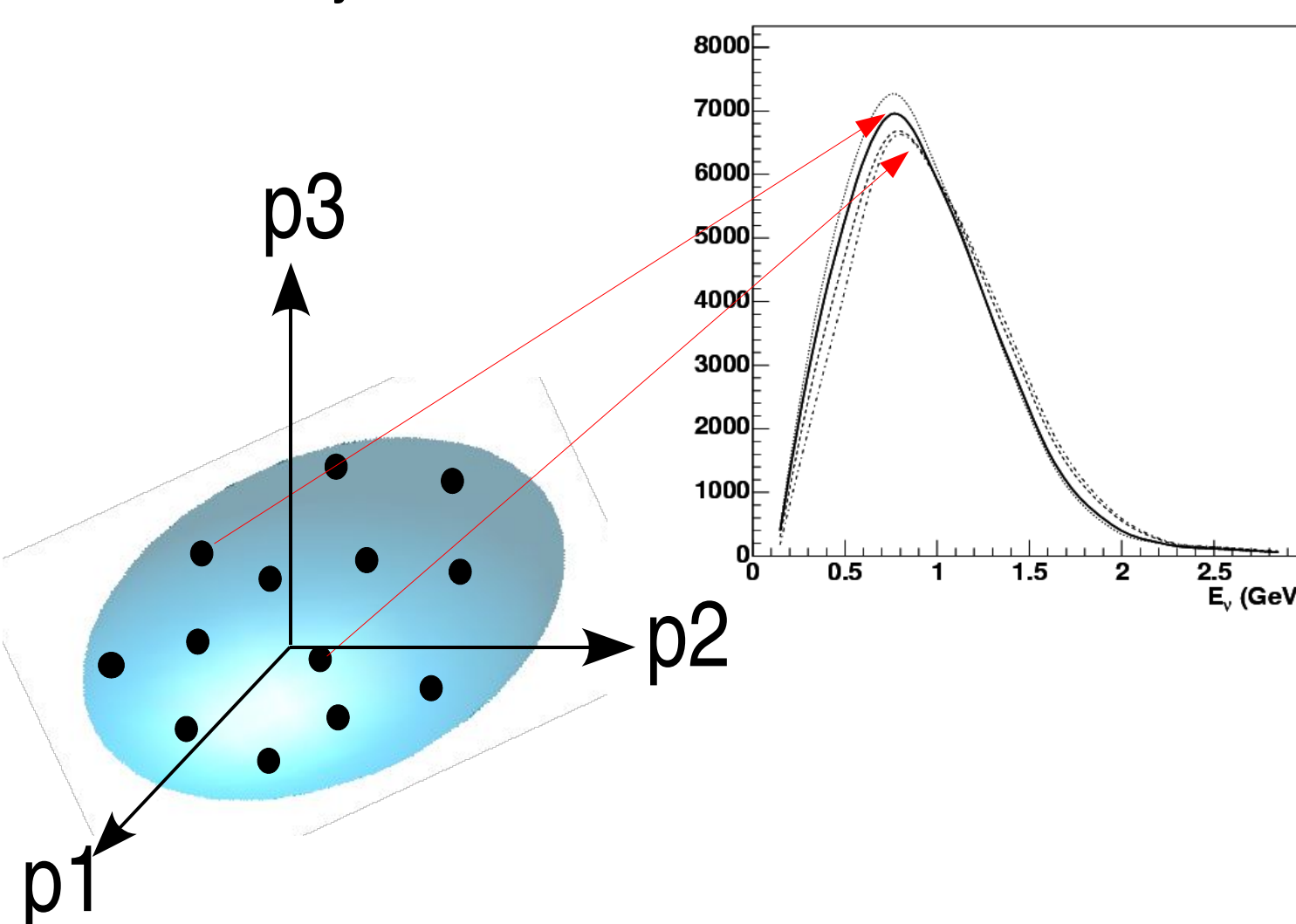
The error Matrix:

The total error matrix is formed by adding together the matrices from the various contributions to the experiment's uncertainty.

For a given contribution to the error we form $N_{mult} = 1000$ (and 67 for the Optical Model) simulations of the neutrino energy distribution in which the relevant parameters have been varied within their estimated covariance. We call these simulations "Multisims".

The parameters associated with a given source of uncertainty are randomly thrown according to their covariance. Each throw produces an effect in the E_{ν}^{QE} distribution.

Uncertainty source "X":



$$M_{ij}^X = \frac{1}{N_{mult} - 1} \sum_{k=1}^{N_{mult}} (N_i^k - N_i^{CV})(N_j^k - N_j^{CV})$$

The total error matrix is constructed by adding the matrices from all the different sources of uncertainty:

$$M_{ij} = \begin{pmatrix} M_{ij}^{\pi^+ \text{ flux}} + M_{ij}^{\pi^- \text{ flux}} + M_{ij}^{K^+ \text{ flux}} + M_{ij}^{K^0 \text{ flux}} + M_{ij}^{Xsec} + M_{ij}^{\pi^0 \text{ rate}} + M_{ij}^{Dirt \text{ rate}} + M_{ij}^{Optical \text{ Model}} + M_{ij}^{Stat} & \begin{pmatrix} \nu_e (s+b) \\ \nu_e / \nu_{\mu} \end{pmatrix} \\ \begin{pmatrix} \nu_e / \nu_{\mu} \\ \nu_{\mu} \end{pmatrix} & \begin{pmatrix} \nu_e / \nu_{\mu} \\ \nu_{\mu} \end{pmatrix} \end{pmatrix}$$

The neutrino energy E_{ν}^{QE} is determined from the scattering angle and energy of the outgoing lepton in a QE interaction. Backgrounds will have mis-reconstructed value for this quantity.

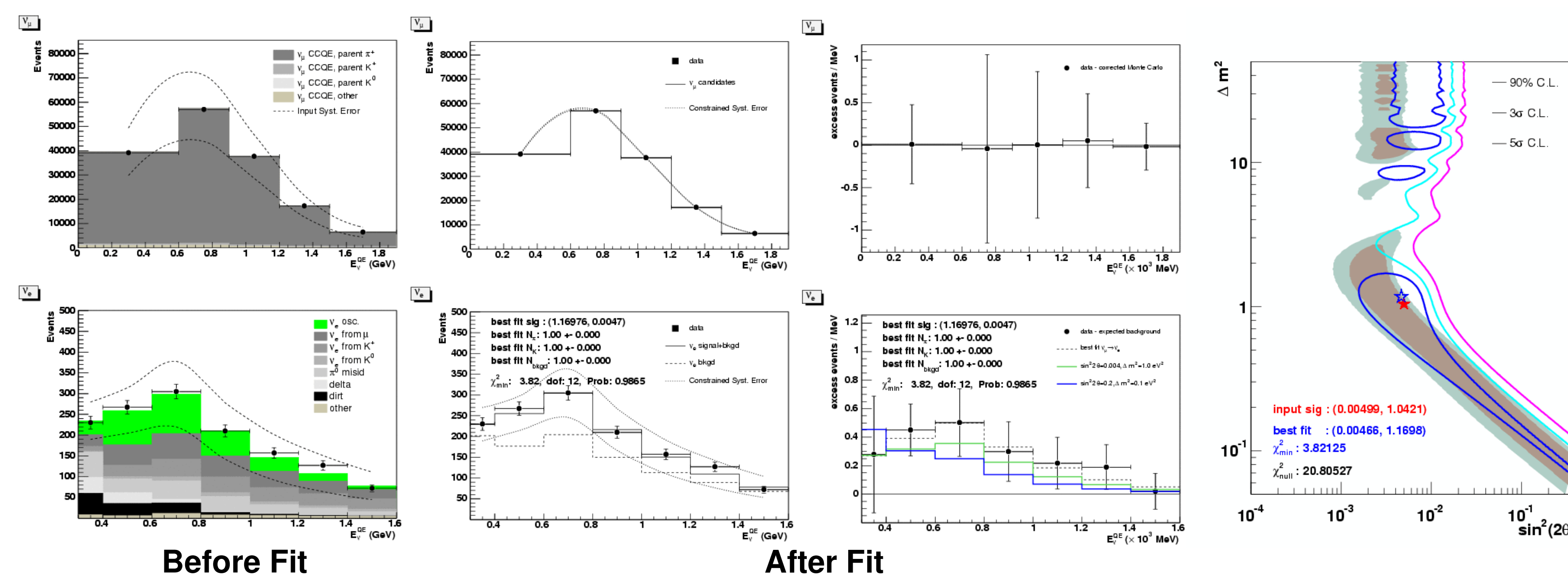
Fit to fake data with strong signal:

Fake data is a statistical fluctuation of the Monte Carlo prediction. The unconstrained errors from Monte Carlo "multisims" are large. An LSND-like signal is added.

The fit constrains the errors and re-shapes the distributions due to the high statistics of the ν_{μ} data set and the $\nu_{\mu} \rightarrow \nu_e$ correlations in the matrix.

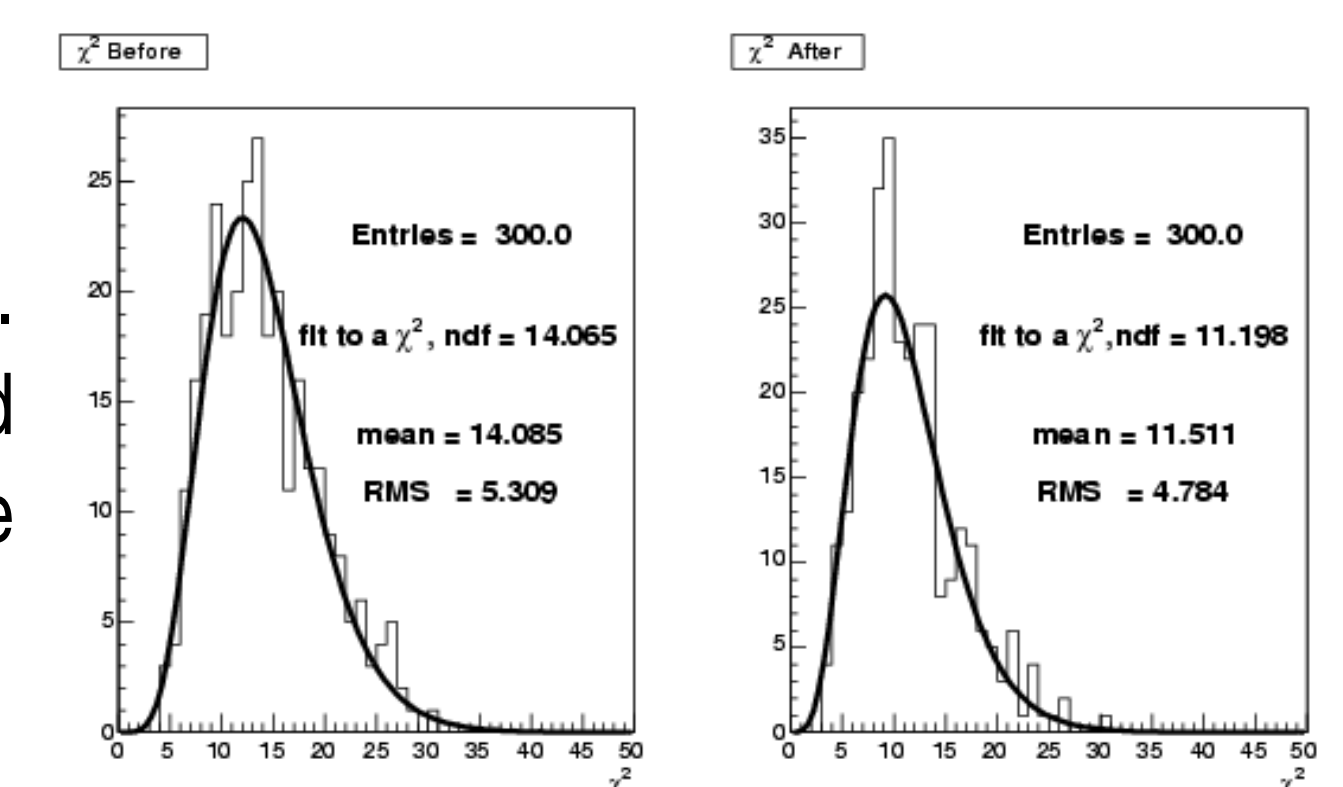
The excess of events can be compared for two possible LSND-like solutions. Here the points have the total errors.

The result of the fit is displayed in the oscillations parameter space.



Statistical robustness:

For fake data sets containing stat+syst. fluctuations, the χ^2 values before and after the fits are consistent with the number of *d.o.f.*: 14 before, 12 after.



Systematic uncertainties:

Source of uncertainty on ν_e background	TBA / BDT (error in %)	Checked or constrained by MiniBooNE data	Further reduced by tying ν_e to ν_{μ}
Flux from π^+/μ^+	6.2 / 4.3	✓	✓
Flux from K^+ decay	3.3 / 1.0	✓	✓
Flux from K^0 decay	1.5 / 0.4	✓	✓
Target and beam models	2.8 / 1.3	✓	✓
ν -cross section	12.3 / 10.5	✓	✓
NC π^0 yield	1.8 / 1.5	✓	✓
External Interactions ("Dirt")	0.8 / 3.4	✓	✓
Optical Model	6.1 / 10.5	✓	✓
DAQ electronics model	7.5 / 10.8	✓	✓

TBA: Track Based analysis (official published result) arXiv:0704.1500 [hep-ex], 2007
BDT: Boosted Decision Tree analysis

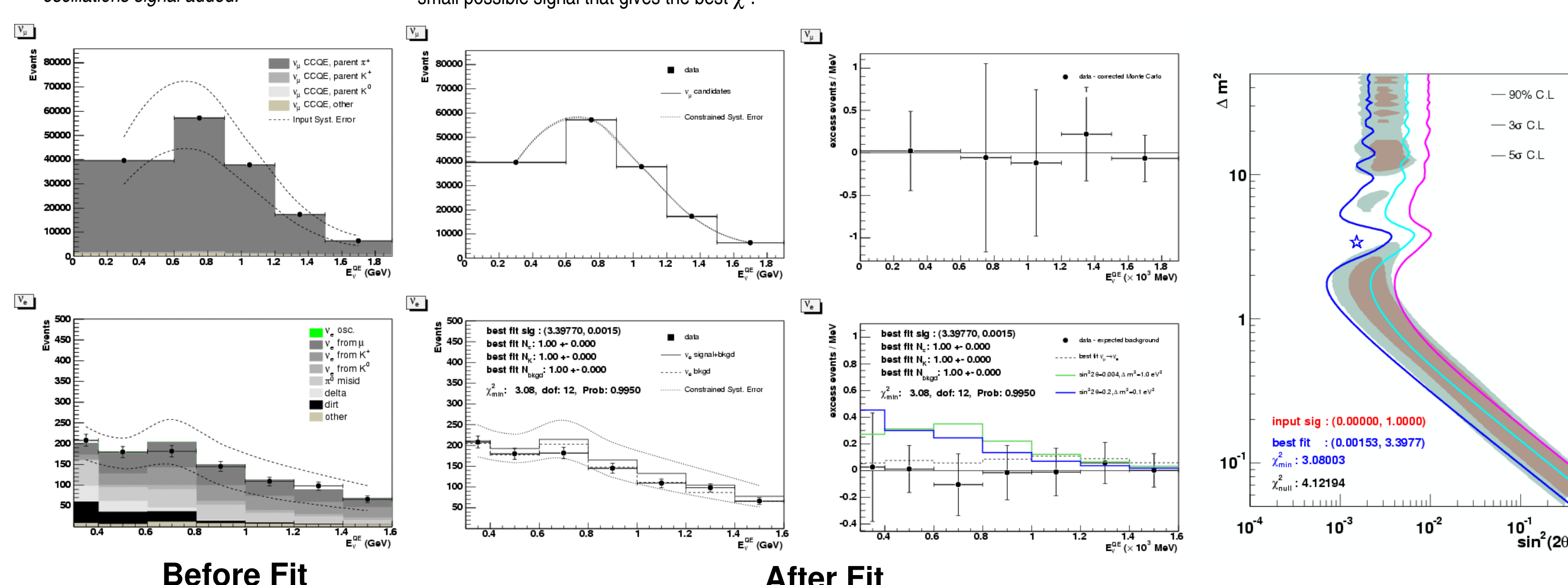
Fit to fake data with no signal (setting a limit):

Fake data is a statistical fluctuation of the Monte Carlo prediction. Unconstrained errors from Monte Carlo "multisims". No oscillations signal added.

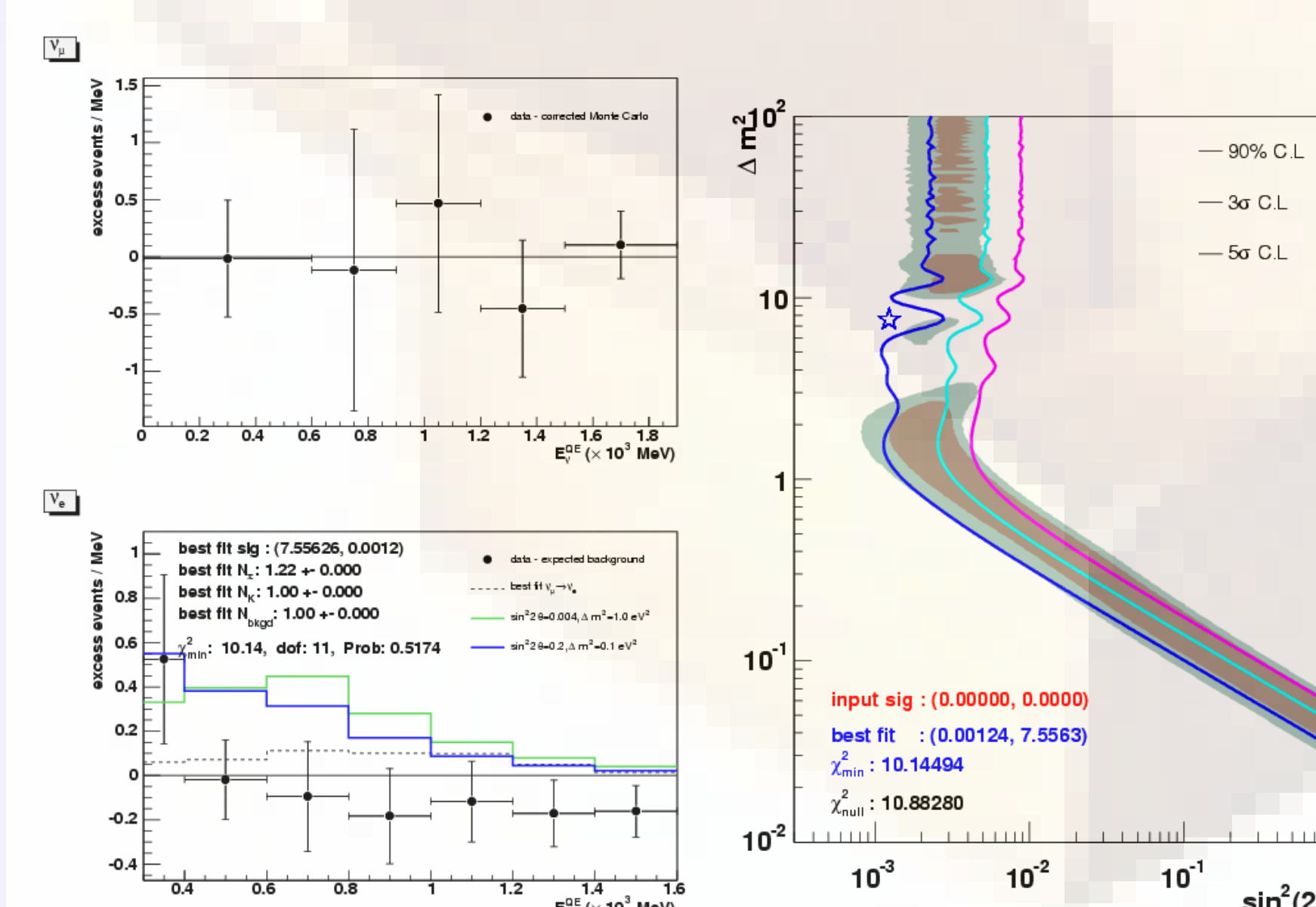
After the fit, the errors have been constrained by the high statistics of the ν_{μ} data set. Fake data is consistent with no signal. The fit picks a small possible signal that gives the best χ^2 .

The excess plot shows the result in a similar way. The points have total errors.

This allows us to set a limit by making a 1-dimensional fit to $\sin^2 2\theta$ for every Δm^2 (raster scan method).



Fit to the MiniBooNE data:



In the fit to the data the ν_{μ} Monte Carlo is scaled by 1.22 to match the data normalization. This scaling factor is allowed by the unconstrained ν_{μ} uncertainties.

The MiniBooNE result is a limit to 2-neutrino oscillations.

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